## MA3K0-15 High-Dimensional Probability

## 23/24

## Department

Warwick Mathematics Institute
Level
Undergraduate Level 3
Module leader
Stefan Adams
Credit value
15
Assessment
Multiple

## Study location

University of Warwick main campus, Coventry

## Description

## Introductory description

N/A
Module web page

## Module aims

- Concentration of measure problem in high dimensions
- Three basic concentration inequalities
- Application of basic variational principles
- Concentration of the norm
- Dependency structures
- Introduction to random matrices


## Outline syllabus

This is an indicative module outline only to give an indication of the sort of topics that may be covered. Actual sessions held may differ.

- Preliminaries on Random Variables (limit theorems, classical inequalities, Gaussian models,

Monte Carlo)

- Basic Information theory (entropy; Kull-Back Leibler information divergence)
- Concentrations of Sums of Independent Random Variables
- Random Vectors in High Dimensions
- Random Matrices
- Concentration with Dependency structures
- Deviations of Random Matrices and Geometric Consequences
- Graphical models and deep learning


## Learning outcomes

By the end of the module, students should be able to:

- Understand the concentration of measure problem in high dimensions
- Be able to distinguish three basic concentration inequalities
- Be able to distinguish between concentration for independent families as well as for various dependency structures
- Understanding of basic concentrations of the norm
- Familiar with random matrices (main properties)
- Be familiar with some application of graphical models
- Be able to understand basic variational problems


## Indicative reading list

We won't follow a particular book and will provide lecture notes. The course is based on the following three books where the majority is taken from [1]:
[1] Roman Vershynin, High-Dimensional Probability: An Introduction with Applications in Data Science, Cambridge Series in Statistical and Probabilistic Mathematics, (2018).
[2] Kevin P. Murphy, Machine Learning - A Probabilistic Perspective, MIT Press (2012).
[3] Simon Rogers and Mark Girolami, A first course in Machine Learning, CRC Press (2017).
[4] Alex Kulesza and Ben Taskar, Determinantal point processes for machine learning, Lecture Notes (2013).

## Subject specific skills

- Understanding that the concentration of measure problem requires analytical expertise as well as some basic probability
- Be able to distinguish three basic concentration inequalities
- Be able to distinguish between concentration for independent families as well as for various dependency structures
- Understanding of basic concentrations of the norm
- Familiar with random matrices (main properties)
- Be familiar with some application of graphical models


## Transferable skills

Students will acquire key reasoning and problem solving skills which will empower them to

## Study

## Study time

| Type | Required |
| :--- | :--- |
| Lectures | 30 sessions of 1 hour $(77 \%)$ |
| Seminars | 9 sessions of 1 hour $(23 \%)$ |
| Total | 39 hours |

## Private study description

No private study requirements defined for this module.

## Costs

No further costs have been identified for this module.

## Assessment

You do not need to pass all assessment components to pass the module.

## Assessment group D1

|  | Weighting | Study time |
| :--- | :--- | :--- |
| Written homework | $15 \%$ |  |
| Written homework (4 example sheets) |  |  |
| In-person Examination | $85 \%$ |  |

- Answerbook Gold (24 page)


## Assessment group R

|  | Weighting | Study time |
| :--- | :--- | :--- |
| In-person Examination - Resit | $100 \%$ |  |

- Answerbook Gold (24 page)


## Feedback on assessment

Marked homework and exam feedback.
Past exam papers for MA3K0

## Availability

## Courses

This module is Optional for:

- Year 1 of TMAA-G1PE Master of Advanced Study in Mathematical Sciences
- Year 1 of TMAA-G1PD Postgraduate Taught Interdisciplinary Mathematics (Diploma plus MSc)
- Year 1 of TMAA-G1PC Postgraduate Taught Mathematics (Diploma plus MSc)
- UCSA-G4G1 Undergraduate Discrete Mathematics

Year 3 of G4G1 Discrete Mathematics
Year 3 of G4G1 Discrete Mathematics

- Year 3 of UCSA-G4G3 Undergraduate Discrete Mathematics
- Year 4 of UCSA-G4G4 Undergraduate Discrete Mathematics (with Intercalated Year)
- Year 4 of UCSA-G4G2 Undergraduate Discrete Mathematics with Intercalated Year
- USTA-G300 Undergraduate Master of Mathematics,Operational Research,Statistics and Economics

Year 3 of G300 Mathematics, Operational Research, Statistics and Economics
Year 4 of G300 Mathematics, Operational Research, Statistics and Economics
This module is Core option list B for:

- UMAA-GV17 Undergraduate Mathematics and Philosophy

Year 3 of GV17 Mathematics and Philosophy
Year 3 of GV17 Mathematics and Philosophy
Year 3 of GV17 Mathematics and Philosophy

- Year 3 of UMAA-GV19 Undergraduate Mathematics and Philosophy with Specialism in Logic and Foundations

This module is Core option list D for:

- UMAA-GV18 Undergraduate Mathematics and Philosophy with Intercalated Year Year 4 of GV18 Mathematics and Philosophy with Intercalated Year
Year 4 of GV18 Mathematics and Philosophy with Intercalated Year
- Year 4 of UMAA-GV19 Undergraduate Mathematics and Philosophy with Specialism in Logic and Foundations

This module is Option list $A$ for:

- TMAA-G1PD Postgraduate Taught Interdisciplinary Mathematics (Diploma plus MSc) Year 1 of G1PD Interdisciplinary Mathematics (Diploma plus MSc)
Year 2 of G1PD Interdisciplinary Mathematics (Diploma plus MSc)
- Year 1 of TMAA-G1P0 Postgraduate Taught Mathematics
- TMAA-G1PC Postgraduate Taught Mathematics (Diploma plus MSc)
- Year 1 of G1PC Mathematics (Diploma plus MSc)
- Year 2 of G1PC Mathematics (Diploma plus MSc)
- UMAA-G105 Undergraduate Master of Mathematics (with Intercalated Year) Year 3 of G105 Mathematics (MMath) with Intercalated Year
Year 4 of G105 Mathematics (MMath) with Intercalated Year
Year 5 of G105 Mathematics (MMath) with Intercalated Year
- UMAA-G100 Undergraduate Mathematics (BSc)

Year 3 of G100 Mathematics
Year 3 of G100 Mathematics
Year 3 of G100 Mathematics

- UMAA-G103 Undergraduate Mathematics (MMath)

Year 3 of G100 Mathematics
Year 3 of G103 Mathematics (MMath)
Year 3 of G103 Mathematics (MMath)
Year 4 of G103 Mathematics (MMath)
Year 4 of G103 Mathematics (MMath)

- UMAA-G106 Undergraduate Mathematics (MMath) with Study in Europe Year 3 of G106 Mathematics (MMath) with Study in Europe
Year 4 of G106 Mathematics (MMath) with Study in Europe
- Year 4 of USTA-G1G3 Undergraduate Mathematics and Statistics (BSc MMathStat)
- Year 5 of USTA-G1G4 Undergraduate Mathematics and Statistics (BSc MMathStat) (with Intercalated Year)
- USTA-GG14 Undergraduate Mathematics and Statistics (BSc)

Year 3 of GG14 Mathematics and Statistics
Year 3 of GG14 Mathematics and Statistics

- Year 4 of UMAA-G101 Undergraduate Mathematics with Intercalated Year
- USTA-Y602 Undergraduate Mathematics,Operational Research,Statistics and Economics Year 3 of Y602 Mathematics,Operational Research,Stats,Economics Year 3 of Y602 Mathematics,Operational Research,Stats,Economics
- Year 4 of USTA-Y603 Undergraduate Mathematics,Operational

Research,Statistics,Economics (with Intercalated Year)
This module is Option list B for:

- Year 1 of TMAA-G1PE Master of Advanced Study in Mathematical Sciences
- Year 3 of USTA-G1G3 Undergraduate Mathematics and Statistics (BSc MMathStat)
- Year 4 of USTA-G1G4 Undergraduate Mathematics and Statistics (BSc MMathStat) (with Intercalated Year)
- Year 4 of USTA-GG17 Undergraduate Mathematics and Statistics (with Intercalated Year)

This module is Option list $E$ for:

- USTA-G300 Undergraduate Master of Mathematics, Operational Research,Statistics and Economics

Year 3 of G30D Master of Maths, Op.Res, Stats \& Economics (Statistics with Mathematics Stream)
Year 4 of G30D Master of Maths, Op.Res, Stats \& Economics (Statistics with Mathematics Stream)

- USTA-G301 Undergraduate Master of Mathematics,Operational Research,Statistics and Economics (with Intercalated
- Year 3 of G30H Master of Maths, Op.Res, Stats \& Economics (Statistics with Mathematics Stream)
Year 5 of G30H Master of Maths, Op.Res, Stats \& Economics (Statistics with Mathematics Stream)

