# FP006-30 Statistics and Further Mathematics

# 23/24

## **Department**

Warwick Foundation Studies

Level

Foundation

Module leader

**David Tapp** 

**Credit value** 

30

**Module duration** 

25 weeks

**Assessment** 

50% coursework, 50% exam

**Study location** 

University of Warwick main campus, Coventry

# **Description**

# Introductory description

FP006-30 Statistics and Further Mathematics

# Module aims

To develop the students' understanding of statistics and further mathematics to enable progression onto undergraduate degree programmes.

To develop an understanding of how statistics and further mathematics can be used in different areas of study and to use them as an effective means of communication.

# **Outline syllabus**

This is an indicative module outline only to give an indication of the sort of topics that may be covered. Actual sessions held may differ.

**Statistics** 

#### Numerical measures

- Standard deviation and variance calculated on ungrouped and grouped data
- · Choice of numerical measures; mean, median, mode, range and interquartile range

## Correlation and regression

- Calculation and interpretation of the product moment correlation coefficient
- Identification of response (dependent) and explanatory (independent) variables in regression
- Calculation of least squares regression lines with one explanatory variable. Scatter diagrams and drawing a regression line theorem
- · Calculation of residuals

# Probability

- Addition law of probability, mutually exclusive events
- Multiplication law of probability and conditional probability, independent events.

## Discrete Random Variables

- Discrete random variables and their associated probability distributions
- Mean, variance and standard deviation
- Mean, variance and standard deviation of a simple function of a discrete random variable

#### **Binomial Distribution**

- · Calculation of probability using formula
- · Use of tables
- · Mean, variance and standard deviation of a binomial distribution

#### Geometric Distribution

- Calculation of probability using formula
- Mean, variance and standard deviation of a Geometric distribution

## Poisson Distribution

- Calculation of probability using formula
- Use of tables
- Mean, variance and standard deviation of a Poisson distribution
- Use the Poisson distribution to approximate binomial distributions

#### Continuous Random Variables

- Differences from discrete random variables
- Probability density functions, cumulative distribution functions and their relationship
- The probability of an observation lying in a specified interval
- · Quartiles and percentiles
- Mean, variance and standard deviation
- Mean, variance and standard deviation of a simple function of continuous random variable

## Continuous Uniform (Rectangular) Distribution

- · General probability density function and cumulative distribution function
- Mean, variance and standard deviation

#### Normal Distribution

- Continuous random variables
- Properties of normal distributions
- · Calculation of probabilities
- Mean, variance and standard deviation of a normal distribution
- Use the normal distribution to approximate binomial and Poisson distributions

## **Further Mathematics**

#### **Matrices**

- Addition, subtraction and multiplication, inverse (2x2 and 3x3).
- Solving linear systems using inverse matrix method.
- Determinants (2x2 and 3x3).
- · Solutions of simultaneous equations using Cramer's rule.
- · Linear transformations.
- Matrix algebra, identity matrices.
- Reversing transformations using inverse matrix method.
- Calculating area enlargement scale factors using determinants.

#### Vectors

- · Vector equations of lines.
- Intersection of lines
- · Distance between lines: parallel and skew
- Dot product.
- · Vector product. Application to area of triangle and parallelogram in 3d.
- Scalar triple product. Application to volume of parallelepiped and tetrahedron
- Vector equation of the plane.
- Intersection of a line and a plane
- Intersection of two planes

#### Partial Differentiation:

- · Functions of several variables.
- · Partial derivatives of functions of several variables.
- · Directional derivatives.
- · Total derivatives.
- Higher partial derivatives.
- Maxima, minima and saddle points.
- Lagrange multiplier method.
- Unconstrained optimization in economics.
- Constrained optimization in economics.

## First Order Differential Equations

- Solving homogeneous first order differential equations.
- Solving linear first order differential equations using an integrating factor.
- Solving exact and non-exact first order differential equations.

## Second Order Differential Equations

- Solutions of homogeneous second order differential equations.
- Solution of non-homogeneous second order differential equations by particular integrals.

## Maclaurin and Taylor Series

- · Maclaurin series. Standard series expansions.
- Taylor series expansions.
- Series solution to a differential equations.

# Learning outcomes

By the end of the module, students should be able to:

- Analyse problems and use mathematical and statistical knowledge to plan strategies for solving them;
- Select and apply a range of mathematical and statistical tools and techniques that are appropriate to solve a given problem;
- Create and use appropriate mathematical and statistical models to solve and understand practical real-life problems, in appropriate contexts;
- Construct and present arguments through appropriate use of logical deduction and precise statements involving correct use of symbols and appropriate statistical and further mathematical language;
- Evaluate the outcomes and predictions of a mathematical or statistical model by considering any assumptions made, and its validity and limitations.

# Indicative reading list

#### **Statistics**

Crawshaw, D.J. and Chambers, J.S. (2001) A Concise Course in Advanced Level Statistics (4th ed.) Nelson Thornes

## Mathematics

C. M. McGregor; J. J. C. Nimmo; W. W. Stothers (2010) Fundamentals of university mathematics, (3rd ed.) Woodhead.

Gaulter, B. and Gaulter, M. (2001) Further pure mathematics. Oxford University Press.

View reading list on Talis Aspire

# Subject specific skills

Mathematical Skills

**Analytical Skills** 

Problem-solving skills

# Transferable skills

Mathematical Skills

**Analytical Skills** 

Problem-solving skills

Communication Skills

# **Study**

# Study time

Туре	Required	
Lectures	25 sessions of 1 hour (8%)	
Seminars	75 sessions of 1 hour (25%)	
Online learning (independent)	25 sessions of 1 hour (8%)	
Private study	115 hours (38%)	
Assessment	60 hours (20%)	
Total	300 hours	

# Private study description

Students are expected to watch "seminar preparation videos" prior to each seminar.

Students are expected to review seminar work after the sessions and also complete the series of Independent Study Questions provided on Moodle.

# Costs

No further costs have been identified for this module.

# **Assessment**

You must pass all assessment components to pass the module.

# **Assessment group C**

	Weighting	Study time	Eligible for self-	
			certification	
Class Test 1	25%	15 hours	No	

Students complete short-answer questions, covering "Statistics" topics, under timed test conditions.

Class Test 2 25% 15 hours No

Students complete short-answer questions, covering "Further Mathematics" topics, under timed test conditions.

In-person Examination 50% 30 hours No

Students complete questions under timed test conditions across all topics of the module, including some which may require them to link multiple topics together and some which may be longer worded problems with real-world contexts.

- Answerbook Pink (12 page)
- Students may use a calculator

#### Feedback on assessment

Written feedback provided on scripts and Tabula.

Past exam papers for FP006

# **Availability**

# **Courses**

This module is Core for:

- FIOE Warwick International Foundation Programme
  - Year 1 of FP18 Warwick International Foundation Programme Computer Science
  - Year 1 of FP17 Warwick International Foundation Programme Economics
  - Year 1 of FP13 Warwick International Foundation Programme Mathematics and Economics
  - Year 1 of FP16 Warwick International Foundation Programme Mathematics and Statistics