# MA249-12 Algebra II: Groups and Rings

#### 22/23

#### **Department**

Warwick Mathematics Institute

Level

Undergraduate Level 2

Module leader

Nicholas Jackson

**Credit value** 

12

**Module duration** 

10 weeks

**Assessment** 

Multiple

**Study location** 

University of Warwick main campus, Coventry

# **Description**

# Introductory description

This is an introductory abstract algebra module. As the title suggests, the two main objects of study are groups and rings.

Module web page

#### Module aims

To study abstract algebraic structures, their examples and applications.

## **Outline syllabus**

This is an indicative module outline only to give an indication of the sort of topics that may be covered. Actual sessions held may differ.

- Groups, subgroups and normal subgroups, rings and fields.
- Isomorphisms, homomorphisms, direct products and quotients for both groups and rings.
- Examples of groups including cyclic, dihedral, symmetric and alternating groups, additive and multiplicative groups of a ring, and general linear groups over a field.

- Generators and relations for groups.
- Order of an element, cosets, Lagrange's theorem, Euler's theorem.
- First, second and third isomorphism theorems and the correspondence theorem for groups.
- Group actions, the Orbit-Stabiliser theorem, conjugacy classes and centralisers.
- Conjugacy classes in symmetric and alternating groups, simplicity of A5.
- Chinese Remainder Theorem.
- First isomorphism theorem and correspondence theorem for rings.
- Ideals, maximal ideals, domains and field of fractions.
- Unique factorisation domains, principal ideal domains, prime and irreducible elements.
- Factorisation in polynomial rings, remainder theorem for polynomials over a field, Gauss's Lemma and Eisenstein's criterion.

## Learning outcomes

By the end of the module, students should be able to:

Recall definitions, theorems and proofs of syllabus material. Calculate with examples of
groups and rings and solve problems using algebraic techniques. Recognise, classify and
construct examples of groups and rings with specified properties by applying the concepts
listed in the syllabus. Apply the orbit-stabiliser theorem to conjugacy classes and
centralisers, as well as to examples from number theory, geometry and combinatorics.

### Indicative reading list

Niels Lauritzen, Concrete Abstract Algebra, Cambridge University Press.

#### Subject specific skills

Students will improve their skills in thinking algebraically in a variety of settings.

This includes working with axiomatic definitions of algebraic objects and analysing the structure and relationships between algebraic objects using fundamental tools such as subobjects and homomorphisms, laying a foundation for future study in algebra, number theory and algebraic geometry.

#### Transferable skills

The module emphasises the power of generalisation and abstraction.

Students will improve their ability to analyse abstract concepts and to solve problems by selecting and applying appropriate abstract tools.

# Study

# Study time

Required

Lectures 30 sessions of 1 hour (25%)
Tutorials 9 sessions of 1 hour (8%)

Other activity 10 hours (8%)
Private study 71 hours (59%)

Total 120 hours

# **Private study description**

Review lectured material and work on set exercises.

# Other activity description

Collaborative project

## Costs

No further costs have been identified for this module.

#### **Assessment**

You do not need to pass all assessment components to pass the module.

Students can register for this module without taking any assessment.

# **Assessment group D1**

	Weighting	Study time
Assignments	15%	
In-person Examination	85%	
2 hour exam, no books allowed		

• Answerbook Pink (12 page)

# Assessment group R

Weighting Study time
In-person Examination - Resit 100%

Answerbook Pink (12 page)

## Assessment group S

	Weighting	Study time
Assignments	15%	
In-person Examination	85%	

Answerbook Pink (12 page)

#### Feedback on assessment

Marked coursework and exam feedback.

Past exam papers for MA249

# **Availability**

#### **Courses**

This module is Core for:

- Year 2 of UMAA-G105 Undergraduate Master of Mathematics (with Intercalated Year)
- UMAA-G100 Undergraduate Mathematics (BSc)
  - Year 2 of G100 Mathematics
  - Year 2 of G100 Mathematics
  - Year 2 of G100 Mathematics
- UMAA-G103 Undergraduate Mathematics (MMath)
  - Year 2 of G100 Mathematics
  - Year 2 of G103 Mathematics (MMath)
  - Year 2 of G103 Mathematics (MMath)
- Year 2 of UMAA-G106 Undergraduate Mathematics (MMath) with Study in Europe
- Year 2 of UMAA-G1NC Undergraduate Mathematics and Business Studies
- Year 2 of UMAA-G1N2 Undergraduate Mathematics and Business Studies (with Intercalated Year)
- Year 2 of UMAA-G101 Undergraduate Mathematics with Intercalated Year

This module is Core optional for:

- UMAA-GV17 Undergraduate Mathematics and Philosophy
  - Year 2 of GV17 Mathematics and Philosophy
  - Year 2 of GV17 Mathematics and Philosophy
  - Year 2 of GV17 Mathematics and Philosophy
- UMAA-GV18 Undergraduate Mathematics and Philosophy with Intercalated Year
  - Year 2 of GV18 Mathematics and Philosophy with Intercalated Year
  - Year 2 of GV18 Mathematics and Philosophy with Intercalated Year

#### This module is Optional for:

- USTA-G300 Undergraduate Master of Mathematics, Operational Research, Statistics and Economics
  - Year 3 of G300 Mathematics, Operational Research, Statistics and Economics
  - Year 4 of G300 Mathematics, Operational Research, Statistics and Economics
- USTA-G1G3 Undergraduate Mathematics and Statistics (BSc MMathStat)
  - Year 2 of G1G3 Mathematics and Statistics (BSc MMathStat)
  - Year 3 of G1G3 Mathematics and Statistics (BSc MMathStat)
  - Year 4 of G1G3 Mathematics and Statistics (BSc MMathStat)
- USTA-G1G4 Undergraduate Mathematics and Statistics (BSc MMathStat) (with Intercalated Year)
  - Year 4 of G1G4 Mathematics and Statistics (BSc MMathStat) (with Intercalated Year)
  - Year 5 of G1G4 Mathematics and Statistics (BSc MMathStat) (with Intercalated Year)
- USTA-GG14 Undergraduate Mathematics and Statistics (BSc)
  - Year 2 of GG14 Mathematics and Statistics
  - Year 2 of GG14 Mathematics and Statistics
- USTA-Y602 Undergraduate Mathematics, Operational Research, Statistics and Economics
  - Year 2 of Y602 Mathematics, Operational Research, Stats, Economics
  - Year 2 of Y602 Mathematics, Operational Research, Stats, Economics

#### This module is Core option list B for:

 Year 3 of UMAA-GV19 Undergraduate Mathematics and Philosophy with Specialism in Logic and Foundations

#### This module is Core option list C for:

 Year 2 of UMAA-GV19 Undergraduate Mathematics and Philosophy with Specialism in Logic and Foundations

#### This module is Option list A for:

- Year 2 of UMAA-GL11 Undergraduate Mathematics and Economics
- Year 2 of UECA-GL12 Undergraduate Mathematics and Economics (with Intercalated Year)
- Year 2 of UPXA-FG33 Undergraduate Mathematics and Physics (BSc MMathPhys)
- UPXA-GF13 Undergraduate Mathematics and Physics (BSc)
  - Year 2 of GF13 Mathematics and Physics
  - Year 2 of GF13 Mathematics and Physics
- UPXA-FG31 Undergraduate Mathematics and Physics (MMathPhys)
  - Year 2 of FG31 Mathematics and Physics (MMathPhys)
  - Year 2 of FG31 Mathematics and Physics (MMathPhys)

# This module is Option list B for:

- UCSA-G4G1 Undergraduate Discrete Mathematics
  - Year 2 of G4G1 Discrete Mathematics
  - Year 2 of G4G1 Discrete Mathematics
- Year 2 of UCSA-G4G3 Undergraduate Discrete Mathematics

- Year 2 of USTA-G300 Undergraduate Master of Mathematics, Operational Research, Statistics and Economics
- USTA-GG14 Undergraduate Mathematics and Statistics (BSc)
  - Year 3 of GG14 Mathematics and Statistics
  - Year 3 of GG14 Mathematics and Statistics
- Year 4 of USTA-GG17 Undergraduate Mathematics and Statistics (with Intercalated Year)
- USTA-Y602 Undergraduate Mathematics, Operational Research, Statistics and Economics
  - Year 2 of Y602 Mathematics, Operational Research, Stats, Economics
  - Year 2 of Y602 Mathematics, Operational Research, Stats, Economics
  - Year 3 of Y602 Mathematics, Operational Research, Stats, Economics
  - Year 3 of Y602 Mathematics, Operational Research, Stats, Economics
- Year 4 of USTA-Y603 Undergraduate Mathematics, Operational Research, Statistics, Economics (with Intercalated Year)

#### This module is Option list E for:

- Year 3 of USTA-G300 Undergraduate Master of Mathematics, Operational Research, Statistics and Economics
- USTA-G301 Undergraduate Master of Mathematics, Operational Research, Statistics and Economics (with Intercalated
  - Year 3 of G30H Master of Maths, Op.Res, Stats & Economics (Statistics with Mathematics Stream)
  - Year 4 of G30H Master of Maths, Op.Res, Stats & Economics (Statistics with Mathematics Stream)