

# ST202-12 Stochastic Processes

**20/21**

**Department**

Statistics

**Level**

Undergraduate Level 2

**Module leader**

Nicholas Tawn

**Credit value**

12

**Module duration**

10 weeks

**Assessment**

Multiple

**Study location**

University of Warwick main campus, Coventry

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## Description

### Introductory description

This module runs in Term 2.

This module is core for students with their home department in Statistics.

It is available as an option or unusual option for other students.

Pre-requisites:

Statistics Students: ST115 Introduction to Probability AND MA137 Mathematical Analysis

Non-Statistics Students: ST111 Probability A AND ST112 Probability B AND (MA131 Analysis I OR MA137 Mathematical Analysis)

Leads to: ST333 Applied Stochastic Processes and ST406 Applied Stochastic Processes with Advanced Topics.

[Module web page](#)

### Module aims

Loosely speaking, a stochastic or random process is any measurable phenomenon which develops randomly in time. Only the simplest models will be considered in this course, namely those where the process moves by a sequence of jumps in discrete time steps. We will discuss:

Markov chains, which use the idea of conditional probability to provide a flexible and widely applicable family of random processes; random walks, which serve as fundamental building blocks for constructing other processes as well as being important in their own right; and renewal theory, which studies processes which occasionally "begin all over again." Such processes are common tools in economics, biology, psychology and operations research, so they are very useful as well as attractive and interesting theories.

The aims of this module are to introduce the idea of a stochastic process, and to show how simple probability and matrix theory can be used to build this notion into a beautiful and useful piece of applied mathematics.

## Outline syllabus

This is an indicative module outline only to give an indication of the sort of topics that may be covered. Actual sessions held may differ.

1. Brief review of fundamental probability notions.
2. Introduction to Markov processes (Definitions, Chapman-Kolmogorov equations, notions of recurrence, transience, positive recurrence, transition probability matrices,
3. Long-run behaviour of Markov Chains, (equilibrium distributions, convergence to equilibrium)
4. Some applications.
5. Discussion of extensions to continuous settings and if time permits to non-Markov settings.

## Learning outcomes

By the end of the module, students should be able to:

- Understand the notion of a Markov chain, and how simple ideas of conditional probability and matrices can be used to give a thorough and effective account of discrete-time Markov chains.
- Understand notions of long-time behaviour including transience, recurrence, and equilibrium.
- Be able to apply these ideas to answer basic questions in several applied situations including genetics, branching processes and random walks.

## Indicative reading list

S.M. Ross, Introduction to Probability Models

G.R. Grimmett and D.R. Stirzaker, Probability and Random Processes

P.W. Jones and P. Smith, Stochastic Processes

J.R. Norris, Markov Chains

[View reading list on Talis Aspire](#)

## Subject specific skills

TBC

## Transferable skills

TBC

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## Study

### Study time

Type	Required	Optional
Lectures	30 sessions of 1 hour (25%)	2 sessions of 1 hour
Tutorials	4 sessions of 1 hour (3%)	
Private study	62 hours (52%)	
Assessment	24 hours (20%)	
Total	120 hours	

### Private study description

Weekly revision of lecture notes and materials, wider reading and practice exercises, working on problem sets and preparing for examination.

### Costs

No further costs have been identified for this module.

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## Assessment

You do not need to pass all assessment components to pass the module.

Students can register for this module without taking any assessment.

### Assessment group D2

	Weighting	Study time	Eligible for self-certification
Multiple Choice Quizzes	10%	12 hours	Yes (waive)
A number of multiple choice quizzes which will take place during the term that the module is delivered.			
Written assignment	10%	12 hours	Yes (extension)
The assignment will contain a number of questions for which solutions and / or written responses			



- Year 2 of USTA-G300 Undergraduate Master of Mathematics, Operational Research, Statistics and Economics
- Year 2 of USTA-G1G3 Undergraduate Mathematics and Statistics (BSc MMathStat)
- Year 2 of USTA-GG14 Undergraduate Mathematics and Statistics (BSc)
- Year 2 of USTA-Y602 Undergraduate Mathematics, Operational Research, Statistics and Economics

This module is Option list A for:

- Year 2 of UCSA-G4G1 Undergraduate Discrete Mathematics
- Year 2 of UCSA-G4G3 Undergraduate Discrete Mathematics
- Year 2 of UMAA-G105 Undergraduate Master of Mathematics (with Intercalated Year)
- Year 2 of UMAA-G100 Undergraduate Mathematics (BSc)
- UMAA-G103 Undergraduate Mathematics (MMath)
  - Year 2 of G100 Mathematics
  - Year 2 of G103 Mathematics (MMath)
- Year 2 of UMAA-G106 Undergraduate Mathematics (MMath) with Study in Europe
- Year 2 of UMAA-G1NC Undergraduate Mathematics and Business Studies
- Year 2 of UMAA-G1N2 Undergraduate Mathematics and Business Studies (with Intercalated Year)
- Year 2 of UMAA-GL11 Undergraduate Mathematics and Economics
- Year 2 of UECA-GL12 Undergraduate Mathematics and Economics (with Intercalated Year)
- Year 2 of UMAA-G101 Undergraduate Mathematics with Intercalated Year